



Investigation of the heavy-flavour hadronization time-scale using the Tsallis-thermometer

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23. Zimányi Winter School 06.12.2023

This work has been supported by the Hungarian NKFIH OTKA FK131979 and K135515 as well as the NKFIH 2021-4.1.2-TÉT-2022-00007 grants.

A non-extensive statistical framework

Identified particle spectrum:

- Low- p_{T} part:
 - soft particle production
 - exponential-like (Boltzmann-Gibbs) distribution
 - stemming from a thermal equilibrium
- High-p_T part:
 - jet-like origin
 - power-law tail distribution
 - described by the perturbative QCD

Tsallis-Pareto distribution smoothly connects the two parts:

$$\left. \frac{\mathrm{d}^2 N}{2\pi p_T \mathrm{d} p_T \mathrm{d} y} \right|_{y \approx 0} = A m_T \left[1 + \frac{q-1}{T} (m_T - m) \right]^{-\frac{q}{q-1}}$$



 $D^0(1864)$ yield in pp collisions at $\sqrt{s} = 5.02$ TeV in |y| < 1.0



1/(2пр_T)d²N/(dp_Tdy) (GeV)⁻²

10-

 10^{-5}

 10^{-7}

2.5

2.0

30

20

ΗH

Motivation for the study

Light-flavoured hadrons (K, π , p, Λ , Φ , Σ , Ξ , Ω) have already been studied in the nonextensive statistical framework in the broad range of collision systems and multiplicities [1] [1] Arxiv:2003.03278

In our study we expand the list of investigated particles with D mesons (containing c quark), which are mostly produced in hard interactions early in the collisions

Our aims are:

- check the feasibility of such a study
- find similarities between light and heavy flavours
- find traces of different production mechanisms and timelines



Investigated datasets

Minimum bias spectra:

- ALICE, pp, 5.02 TeV D⁰, D⁺, D^{*+}
- ALICE, pp, 7 TeV D⁰, D⁺, D^{*+}
- ALICE, pPb, 5.02 TeV D⁰, D⁺, D^{*+}

Centrality (multiplicity) dependent:

- ALICE, PbPb, 2.76 TeV D⁰ centralities: 0-20%, 40-80%
- STAR, AuAu, 200 GeV D^o centralities: 0-10%, 10-20%, 20-40%, 40-60%, 60%-80%



Tsallis-thermometer

Observation: total charged hadron multiplicity in Tsallis theory follows negative binomial distribution

This is also supported by experimental data

Taking fluctuations of the produced particles n:

$$T = \frac{E}{\langle n \rangle},$$
$$q = 1 - \frac{1}{\langle n \rangle} + \frac{\Delta n^2}{\langle n \rangle^2}$$

T and q are correlated:

$$T = E\left(\delta^2 - (q-1)
ight) \qquad rac{\Delta n^2}{\left\langle n
ight
angle^2} \coloneqq \delta^2$$

Observations for the light flavours

- Strong dependence on event multiplicity
- Mass hierarchy, stronger towards heavier particles
- All points aiming towards $T_{eq}{\approx}0.14~GeV$ and $q_{eq}{\approx}1.15$

$$T = E\left(\delta^2 - (q-1)\right)$$



D mesons in the Tsallis theory

- Strong dependence on event multiplicity
- Mass hierarchy is even stronger, than for light flavours
- Dependence on the collision energy is more prominent, than for the light hadrons
- A grouping is also present, however the "center" is shifted compared to the light flavours

$$0.6 \\ f^{(1)} = (0.140) \\ f^{(2)} = (0.493) \\ f^{(2)} = (0.493) \\ f^{(2)} = (0.938) \\ f^{(2)} = (0.333) \\ f^{(2)} = (1.531) \\ f^{(2)} = (1.531)$$

 $T = E\left(\delta^2 - (q-1)\right)$

Tsallis-thermometer

- D mesons reach higher E values
- Fluctuations are stronger on the average

Fitting the E-E δ^2 points with a line defines the equilibrium $\frac{5}{20}$ 1.5 values for the T (offset) and q (slope) parameters.

0

$$T = E\left(\delta^2 - (q-1)\right)$$
 $\frac{\Delta n^2}{\langle n \rangle^2} := \delta^2$

Light flavours: $T_{eq} \approx 0.14$ GeV and $q_{eq} \approx 1.15$ Heavy flavours: $T_{eq} \approx 0.25$ GeV and $q_{eq} \approx 1.21$



Production time-scale differences between light and heavy flavours

Light flavours: $T_{eq} \approx 0.14 \text{ GeV}$ and $q_{eq} \approx 1.15$

Heavy flavours: $T_{eq} \approx 0.25$ GeV and $q_{eq} \approx 1.21$

 $\Delta T_{eq}{\approx}0.11~GeV$

pPb 5.02 TeV:

- $\Delta T(D \text{ meson-pion}) > 0.3 \text{ GeV}$
- ∆T(D meson-proton)>0.2 GeV
- ∆T(D meson-Omega)<0.1 GeV

AuAu 200 GeV:

• ∆T(D meson-light flavour)≈0.10-0.15 GeV



Conclusion

- We extended the non-extensive statistical framework beyond the light flavours
- Broad range of D meson data from ALICE and STAR experiments was used, consisting of 5 different collision systems: from pp to AA, from 200 GeV to 7 TeV, from minimum bias to low and high centralities
- The Tsallis-Pareto fits of the D meson spectra describe precisely both the low- $p_{\rm T}$ and the high- $p_{\rm T}$ regions
- Lot of similar trends to the light-flavour hadrons, however having different scale:
 - dependence on multiplicity and collision systems
 - mass hierarchy
 - overall grouping
- The results show that D mesons indeed interact with a hot medium after being produced in the initial stages of a collision

Thank you for your attention!

Back-up



L. Gyulai, Heavy flavours in Tsallis-thermometer, Zimányi School 2023









Thermodynamical consistency



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