# How far can we see back in time in high-energy collisions using charm hadrons?

HUN

REN

#### G.G. Barnaföldi, L. Gyulai, G. Bíró, R, Vértesi

mailing

Support: Hungarian NKFIH grants K135515, FK13979, 2019-4.1.2-TET-2022-00007, 2021-4.1.2-NEMZ KI-2024-00031, 2021-4.1.2-NEMZ KI-2024-00033 and 2021-4.1.2-NEMZ KI-2024-00034, Wigner Scientific Computing Laboratory

Refs: J.Phys.G 51 (2024) 8, 085103, Submitted to IJMPA (arXiv 2409.01085)

Advances, Innovations, and Future Perspectives in High-energy Nuclear Physics, Wuhan, Hubei, China, 22<sup>nd</sup> October 2024





### How far can we see back in time in HIC?







#### I can see back to 2013, the first time in Wuhan.



.... then 2015 Yaxian & Daizhui....



.... then 2016 Xin Nian, Ben-Wei, Chunbin, Daimei, Keming Shen, Gouyang Ma....



#### .... then HP2017 with many of you....



.... then 2018 Xin Nian et al ....



#### .... then 2019 Lilin Zhu, Keming Shen, Jiang Zefang ....



.... then 2023 Fengyi Zhao, Chao Wu, Jiang Zefang ....

### How far can we see back in time with charm?



Let's focus on "charmly" to the other side of the history....

### Motivation for the talk...

### Our aims here are:

- define a thermometer
- check the feasibility to define a scale



### Motivation for the talk...

### **Our aims here are:**

- define a thermometer
- check the feasibility to define a scale
- find similarities between light and heavy flavours
- find traces of different production mechanisms & timelines

### All within the non-extensive statistical framework



### **Related works**

**Previous studies** (K Shen, G Bíró, TS Biró, AN Mishra, GGB)

Light-flavoured hadrons (K,  $\pi$ , p,  $\Lambda$ ,  $\Phi$ ,  $\Sigma$ ,  $\Xi$ ,  $\Omega$ ) have already been studied in the non-extensive statistical framework in the broad range of collision systems and multiplicities [JPG 47 (2020) 10, 105002, JPG 50 (2023) 9, 095004]

**Recent works** (L Gyulai, R. Vértesi, G. Bíró, G. Paic, GGB)

In our study we expand the list of investigated particles with D mesons (containing c quark), which are mostly produced in hard interactions early in the collisions [JPG 51 (2024) 8, 085103, IJMPA (arXiv:2409.01085)]



### Hadron spectra vs. extensive statistics

Identified particle spectrum:

- Low- $p_T$  part:
  - soft particle production
  - exponential-like (Boltzmann-Gibbs) distr.
  - stemming from a thermal equilibrium



### Hadron spectra vs. non-extensive statistics

Identified particle spectrum:

- Low- $p_T$  part:
  - soft particle production
  - exponential-like (Boltzmann-Gibbs) distr.
  - stemming from a thermal equilibrium
- High- $p_{T}$  part:
  - jet-like origin
  - power-law tail distribution
  - described by the perturbative QCD

**Tsallis-Pareto distribution smoothly connects both:** 

$$\frac{\mathrm{d}^2 N}{2\pi p_T \mathrm{d} p_T \mathrm{d} y} \bigg|_{y \approx 0} = A m_T \left[ 1 + \frac{q-1}{T} (m_T - m) \right]$$



### Quantify and compare LF hadron spectra data

- Precise spectra description
  - from low- to high- $p_{\tau}$

$$f(m_T) = A \cdot \left[ 1 + \frac{q-1}{T_s} (m_T - m) \right]^{-\frac{1}{q-1}}$$

- in multiplicity classes (pp, pA, AA)

$$\frac{\mathrm{dN}_{\mathrm{ch}}}{\mathrm{dy}}\Big|_{y=0} = 2\pi A T_s \left[ \frac{(2-q)m^2 + 2mT_s + 2T_s^2}{(2-q)(3-2q)} \right] \times \left[ 1 + \frac{q-1}{T_s}m \right]^{-\frac{1}{q-1}}$$

- With PID:

 $\pi^{\pm}, K^{\pm}, K^0_s, K^{*0}, p(\bar{p}), \Phi, \Lambda, \Xi^{\pm}, \Sigma^{\pm}, \Xi^0, \Omega$ 

#### - Wide range:

	рр	рА	AA
CM energy (GeV)	7000, 13000	5020	130-5020
Multiplicity range	2.2-25.7	4.3-45	13.4-2047



### Identifying scaling in light flavour hadron spectra

• QCD-inherited scaling properties

$$f(m_T) = A \cdot \left[ 1 + \frac{q-1}{T_s} (m_T - m) \right]^{-\frac{1}{q-1}}$$

- Parameter scaling with  $\sqrt{s} \& \text{multiplicity}$   $A(\sqrt{s_{NN}}, \langle N_{ch}/\eta \rangle, m) = A_0 + A_1 \ln \frac{\sqrt{s_{NN}}}{m} + A_2 \langle N_{ch}/\eta \rangle$   $T(\sqrt{s_{NN}}, \langle N_{ch}/\eta \rangle, m) = T_0 + T_1 \ln \frac{\sqrt{s_{NN}}}{m} + T_2 \ln \ln \langle N_{ch}/\eta \rangle,$  $q(\sqrt{s_{NN}}, \langle N_{ch}/\eta \rangle, m) = q_0 + q_1 \ln \frac{\sqrt{s_{NN}}}{m} + q_2 \ln \ln \langle N_{ch}/\eta \rangle,$ 

- Details:

G. Biró *et al: J.Phys.G 47 (2020) 10, 105002*K. Shen *et al Eur.Phys.J.A 55 (2019) 8, 126*



# Introducing the Tsallis-thermometer



# Introducing the Tsallis-thermometer

QCD-inherited scaling properties

$$f(m_T) = A \cdot \left[ 1 + \frac{q-1}{T_s} (m_T - m) \right]^{-1}$$

- Parameter scaling with  $\sqrt{s}$  & multiplicity A( $\sqrt{s_{NN}}$ ,  $\langle N_{ch}/\eta \rangle$ , m) = A<sub>0</sub> + A<sub>1</sub> ln  $\frac{\sqrt{s_{NN}}}{m}$  + A<sub>2</sub>  $\langle N_{ch}/\eta \rangle$ 

 $T(\sqrt{s_{NN}}, \langle N_{ch}/\eta \rangle, m) = T_0 + T_1 \ln \frac{\sqrt{s_{NN}}}{m} + T_2 \ln \ln \langle N_{ch}/\eta \rangle$ 

 $q(\sqrt{s_{NN}}, \langle N_{ch}/\eta \rangle, m) = q_0 + q_1 \ln \frac{\sqrt{s_{NN}}}{m} + q_2 \ln \ln \langle N_{ch}/\eta \rangle,$ 

- Light Flavour (LF)
  - Strong dependence on event multiplicity
  - Mass hierarchy presents for light flavour
  - LF grouping:  $T_{eq} \approx 0.14$  GeV and  $q_{eq} \approx 1.15$



Non-extensive entropy does not need thermal equilibrium:  $S(E_1 + E_2) \neq S(E_1) + S(E_2)$ 

$$\frac{1}{T} = \left\langle S'(E) \right\rangle = \left\langle \beta \right\rangle$$
$$q = 1 - \frac{1}{C} + \frac{\Delta \beta^2}{\left\langle \beta \right\rangle^2}.$$

Non-extensive entropy does not need thermal equilibrium:  $S(E_1 + E_2) \neq S(E_1) + S(E_2)$ 

 $\frac{1}{T} = \left\langle S'(E) \right\rangle = \left\langle \beta \right\rangle$  $q = 1 - \frac{1}{C} + \frac{\Delta \beta^2}{\left\langle \beta \right\rangle^2}.$ 



Non-extensive entropy does not need thermal equilibrium:  $S(E_1 + E_2) \neq S(E_1) + S(E_2)$ 

 $\frac{1}{T} = \left\langle S'(E) \right\rangle = \left\langle \beta \right\rangle$  $q = 1 - \frac{1}{C} + \frac{\Delta \beta^2}{\left\langle \beta \right\rangle^2}.$ 

$$\begin{split} T &= \frac{E}{\langle n \rangle}, \\ q &= 1 - \frac{1}{\langle n \rangle} + \frac{\Delta n^2}{\langle n \rangle^2} \end{split} \qquad T = E\left(\delta^2 - (q-1)\right) \\ \frac{\Delta n^2}{\langle n \rangle^2} &:= \delta^2 \end{split}$$

Non-extensive entropy does not need thermal equilibrium:  $S(E_1 + E_2) \neq S(E_1) + S(E_2)$ 

 $\frac{1}{T} = \left\langle S'(E) \right\rangle = \left\langle \beta \right\rangle$  $q = 1 - \frac{1}{C} + \frac{\Delta \beta^2}{\left\langle \beta \right\rangle^2}.$ 



Non-extensive entropy does not need thermal equilibrium:  $S(E_1 + E_2) \neq S(E_1) + S(E_2)$ 

 $\frac{1}{T} = \left\langle S'(E) \right\rangle = \left\langle \beta \right\rangle$  $q = 1 - \frac{1}{C} + \frac{\Delta \beta^2}{\left\langle \beta \right\rangle^2}.$ 





Transforming the Tsallis-thermometer and fitting the *E-E* $\delta^2$  points with a line defines the (linearized) equilibrium values for the: *T* (offset) and *q* (slope) parameters.

# Tsallis-thermometer of light flavours

#### Light Flavour (LF)

- Strong dependence on event multiplicity
- Mass hierarchy presents for LF
- LF grouping:  $T_{eq} \approx 0.14$  GeV and  $q_{eq} \approx 1.15$



### Light Flavour (LF)

- Strong dependence on event multiplicity
- Mass hierarchy presents for LF
- LF grouping:  $T_{eq} \approx 0.14$  GeV and  $q_{eq} \approx 1.15$

- Dependence on the collision energy for HF of is more prominent, than for LF
- A HF grouping is also present, however the <sub>0.1</sub> "center" is shifted compared to the LF
- HF grouping:  $T_{eq} \approx 0.25$  GeV and  $q_{eq} \approx 1.21$



### Light Flavour (LF)

- Strong dependence on event multiplicity
- Mass hierarchy presents for LF
- LF grouping:  $T_{eq} \approx 0.14$  GeV and  $q_{eq} \approx 1.15$

- Dependence on the collision energy for HF 0.2 is more prominent, than for LF
- A HF grouping is also present, however the <sub>0.1</sub> "center" is shifted compared to the LF
- HF grouping:  $T_{eq} \approx 0.25$  GeV and  $q_{eq} \approx 1.21$



### Light Flavour (LF)

- Strong dependence on event multiplicity
- Mass hierarchy presents for LF
- LF grouping:  $T_{eq} \approx 0.14$  GeV and  $q_{eq} \approx 1.15$

- Dependence on the collision energy for HF 0.2 is more prominent, than for LF
- A HF grouping is also present, however the <sub>0.1</sub> "center" is shifted compared to the LF
- HF grouping:  $T_{eq} \approx 0.25$  GeV and  $q_{eq} \approx 1.21$



### Light Flavour (LF)

- Strong dependence on event multiplicity
- Mass hierarchy presents for LF
- LF grouping:  $T_{eq} \approx 0.14$  GeV and  $q_{eq} \approx 1.15$

- Dependence on the collision energy for HF is more prominent, than for LF
- A HF grouping is also present, however the "center" is shifted compared to the LF
- HF grouping:  $T_{eq} \approx 0.25$  GeV and  $q_{eq} \approx 1.21$



#### **Further properties of the fix point**

- Temperature  $(T_{eq})$  of the common fix points for mesons are linearly increase with the hadron masses.
- Temperature,  $T_{eq}$  is smaller for baryons than the same mass mesons.
- Non-extensivity parameter,  $q_{eq}$  does not present significant mass dependence



- Bjorken-model DOES NOT say anything on the thermodynamical description
  - → temperature scales can be connected

 $\tau = \tau_0 \left(\frac{T_0}{T}\right)^3$ 

Once we know the temperature values, we could turn this to measure the time scales, using the approximated fix point value: T<sub>eq</sub>

$$\tau_{\rm D} = \tau_{\rm LF} \left(\frac{T_{\rm LF}}{T_{\rm D}}\right)^3$$

Taking all light flavours as reference,
 → D-meson formation relative to all LF



- Bjorken-model DOES NOT say anything on the thermodynamical description
  - → temperature scales can be connected

 $\tau = \tau_0 \left(\frac{T_0}{T}\right)^3$ 

• Once we know the temperature values, we could turn this to measure the time scales, using the approximated fix point value:  $T_{eq}$ 

$$\tau_{\rm D} = \tau_{\rm LF} \left(\frac{T_{\rm LF}}{T_{\rm D}}\right)^3$$

Taking all light flavours as reference,
 → D-meson formation relative to all LF



#### Adding more identified hadrons

- Pion formation is the latest one
- Formation time has mass order: the lighter the hadron is, it forms later.
- Heavier baryons forms later than other mesons with the same mass
- Taking all PID & D-mesons (here only at LHC energies)  $\rightarrow$  **D-meson formation** relative to  $\pi$  is 30x earlier...



#### **Adding more identified hadrons**

- Pion formation is the latest one
- Formation time has mass order: the lighter the hadron is, it forms later.
- Heavier baryons forms later than other mesons with the same mass
- Taking all PID & D-mesons (here only at LHC energies) → D-meson formation
  relative to π is 30x earlier...



# Conclusions

#### Non-extensive statistical framework

- Based on the data, our model is working for both LF and D-meson production
- Works from RHIC to LHC energies at the highest  $p_T$
- Tsallis-Pareto fits well in all multiplicities

#### Comparing LF & HF via Tsallis-thermometer

- Tsallis-thermometer present similar trends, but scales are different between LF and HF.
- Mass hierarchy is present and stronger for HF
- Overall grouping is different between mesons & baryons, and between LF & HF

→ To take away... Bjorken model is compatible with the Tsallis-thermometer, and relative formation time can be estimated.









### Thermodynamical consistency?

Thermodynamical consistency: fulfilled up to a high degree





Compare EoS to data: Lattice QCD (parton) & Biró-Jakovác parton-hadron



### Thermodynamical consistency?

Thermodynamical consistency: fulfilled up to a high degree



**Compare EoS to data**: Lattice QCD (parton) & Biró-Jakovác parton-hadron











